



# **DNA 4398F**

# INTERACTIONS OF STRESS WAVES WITH DEEPLY-BURIED TUNNELS IN **GEOLOGIES WITH CRACKS AND DISCONTINUITIES**



California Research & Technology, Inc. 6269 Variel Avenue Woodland Hills, California 91367

JANUARY 1976

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Prepared for

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t p d i	The purpose of this study was to examine the response of deeply-buried tunnels to the effects of high stress dynamic loading. In the Phase I portion of the study, attention was concentrated on the effects of geold discontinuities (e.g., joints) on tunnels, with particular emphasis on interactions between joints and backpacking. In Phase II, emphasis was the response of integral tunnels in hard and soft rock geologies, and or implementation of a coupled finite element/finite difference method (cal				

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20. ABSTRACT (Continued)

LAP, for Linked Analysis Program) for analyzing the response of thin liners to dynamic loading in geologic media.

In this report, a summary is provided of the Phase I work, and a more detailed discussion is given of the Phase II effort. Recommendations are made as to work which might be conducted in an on-going program.

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# TABLE OF CONTENTS

1.	INTRODUCTION AND SUMMARY OF RESULTS OF PHASE I	
2.	SUMMARY OF RESULTS OF PHASE II, AND RECOMMENDATIONS	
		1 (
	2.1 Phase II Summary	1 (
	2.2 Recommendations	12
3.	MATERIAL PROPERTIES FOR NUMERICAL SOLUTIONS	1 5
	3.1 Tuff	1 5
	3.1.1 Equation of State	1 5
	3.1.2 Failure	16
	3.2 Granite	19
	3.3 Concrete	19
4.	UNLINED AND CONCRETE-LINED TUNNELS	2]
	4.1 Unlined Tunnel in Granite	2 ]
	4.2 Concrete Liners in Tuff - Comparisons Showing Effects of Different Failure Models	26
		3]
5.	COUPLED FINITE DIFFERENCE/FINITE ELEMENT LAP CODE FOR ANALYSIS OF THIN LINERS	37
6.	DEFORMABLE STEEL LINERS	39
	6.1 Two-Inch Steel Liner in Tuff (Case M)	3 9
	6.2 Two-Inch Steel Liner Backed by Two Feet of Concrete in Tuff (Case N)	4 (
	REFERENCES	12

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### 1. INTRODUCTION AND SUMMARY OF RESULTS OF PHASE I

All rock masses contain large numbers of nominally planar discontinuities, such as joints, faults, cracks, and bedding planes. These surfaces usually have properties which are quite different from the basic medium, and there is both experimental and theoretical evidence to suggest that the effects of these discontinuities should be one of the important considerations involved in designing survivable underground structures.

In extreme cases, the sliding of material along joints or other discontinuities could cut off a buried structure (by guillotining), or it could split a tunnel lengthwise, as shown in the sketches below. In less extreme cases, the situation shown in Figure 1 may develop, where portions of the tunnel wall attempt to project into the tunnel. The tunnel liner must resist such motion. Backpacking, of course, makes it easier for a tunnel liner to accommodate small displacements without damage.



In the Phase I study, interactions of the type shown in Figure 1 between deeply-buried tunnels and in situ joints in granite when loaded by 1 kb stress waves were investigated using both analytical models and two-dimensional finite

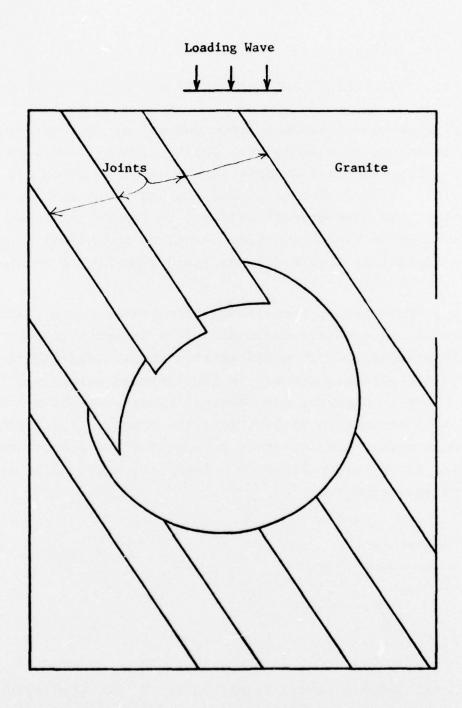


Figure 1. Damage Mode from Local Block Motions Near Tunnels Considered in Phase I of Study

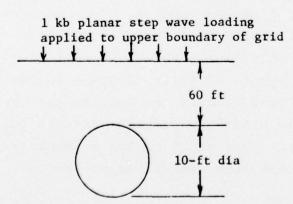
difference numerical code calculations. The study consisted of (1) the development and use of analytical solutions to simplified models to predict if, and where slippage of joints occurs near a tunnel, (2) the development of a model which provides a conservative estimate of the ability of a backpacking system to resist and accommodate block motions, and (3) the generation of seven exploratory numerical solutions (using the Lagrangian WAVE-L finite difference code) to examine the time-resolved wave propagation interactions between various lined and unlined tunnels, with and without joints present in the surrounding rock. The conditions for these numerical solutions in Phase I are listed in Table 1. All of the solutions were two-dimensional, plane strain cases treating a 1 kb planar step wave incident on an infinite cylindrical tunnel. Models were developed for use in the numerical solutions to describe the hydrodynamic, elastic, and failure properties of the backpacking material. Also, constitutive properties were formulated for dilatent rock joints.

Two important, related conclusions can be drawn from the results of the Phase I study:

1. Significant block motions and joint slippage in the immediate vicinity of a tunnel will be primarily activated by stress relief waves emanating from the opening. This activation of joint motions is most likely to occur near the tunnel springlines, but it involves only blocks which are near the tunnel. There may be small amounts of joint slippage in the free field before the stress wave reaches the tunnel, but the tendency for joint slippage is greatly increased near the tunnel due to local stress relief. (It is of course evident that large relative displacements can occur across major fault

Table 1. Conditions for Numerical Solutions in Phase I Portion of Study

Case	Medium	<u>Joints</u>	Backpacking	Liner
A	Granite	None	None	Unlined
В	Granite	~3' spacing, frictionless, ⊥to wave front	None	Unlined
С	Granite	None	5' simulated backpacking	l" rigid steel
D	Granite w/no tensile failure	<pre>3' spacing, diag. to wave, dilatent w/friction</pre>	None	Unlined
Е	Granite	3' spacing, diag. to wave, dilatent w/friction	None	Unlined
F	Granite	3' spacing, diag. to wave, dilatent w/friction	None	l" rigid steel
G	Granite	3' spacing, diag. to wave, dilatent w/friction	5' cellular concrete, P_=1500 psi	3/8" rigid steel



l' nominal zoning used in all problems. Tunnels were at 4000' depth. planes or long planar surfaces with low shear resistance, with or without the presence of a tunnel, but we were not concerned with these large-scale phenomena in this study.)

Backpacking and friction are very effective in limiting these local block motions for 0.5 - 1.5 kb stress loads on deeply-buried tunnels. Figures 2 and 3 show estimates (obtained from an analytical model) of the thicknesses of backpacking required to stop a block of length L which has been accelerated into a tunnel by 0.5, 1.6, and 1.5 kb stress loads. backpacking resists the block penetration with a crushing stress of 1900 psi in uniaxial strain. After the backpacking has sustained 9% strain, it begins to lock up, and stresses rise sharply above 1900 psi. In our conservative model, we assumed that this condition would result in tunnel failure. Figure 2 shows the extreme case of frictionless, or open joints. Even in this worst case, 11 inches of backpacking is sufficient to stop a 10-ft long block accelerated by a 1 kb wave. 25 inches of backpacking are required for a 1.5 kb wave. Figure 3 illustrates the effectiveness of frictional forces acting along the joints bounding the moving block. With a nominal frictional shear stress of 100 bars (which roughly corresponds to a "wet" joint), only 4.5 in. and 10 in., respectively, are required to stop a 10-ft long block accelerated by 1 kb and 1.5 kb waves.

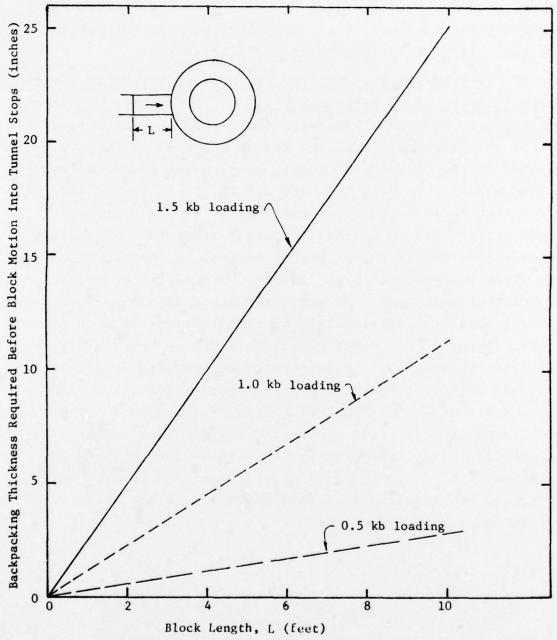


Figure 2. Backpacking Thickness Required to Stop a Block Accelerated into a Tunnel by Stress Loadings of 0.5, 1.0, and 1.5 kb (No friction)

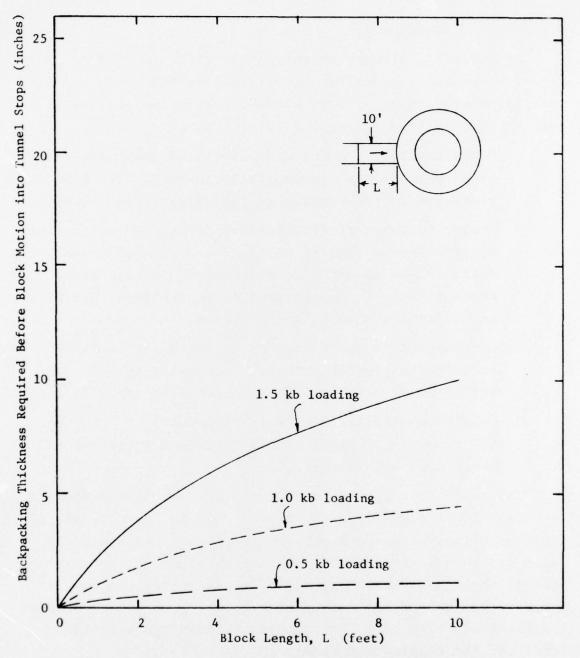


Figure 3. Backpacking Thickness Required to Stop a Block Accelerated into a Tunnel by Stress Loadings of 0.5, 1.0, and 1.5 kb (100 bar frictional stress on sliding surfaces of block)

# 2. SUMMARY OF RESULTS OF PHASE II, AND RECOMMENDATIONS FOR CONTINUING EFFORT

### 2.1 PHASF II SUMMARY

In Phase II, primary attention was given to liners in softer geologic media, as exemplified by NTS tuff, and to integral liners (i.e., liners without porous backpacking). This Phase consisted of the following main efforts:

- o Development of a model and associated numerical technique which allow shear cracks to explicitly form and propagate in the Lagrangian finite difference code,
- o Exploratory numerical solutions to examine effects of dynamic stress loading on lined and unlined tunnels in tuff, and to examine the effects of explicit shear crack failure (as contrasted to conventional plasticity failure) on the tunnel response,
- o Development of the LAP code, a linked finite difference/finite element method, for coupled analysis of the response of thin liners in geologic materials, and
- o Coupled numerical solutions, using LAP, to analyze the response of steel liners (with and without concrete backing) in tuff.

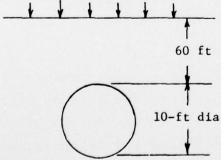
The conditions for the six numerical solutions performed in Phase II are summarized in Table 2. As in Phase I, all of these solutions were two-dimensional, plane strain cases in which the tunnel was subjected to a 1 kb planar step wave. Some of these cases were exercising or demonstrating new aspects of the analytical methods for treating buried structures for the first time (i.e., the explicit shear crack failure model and the coupled LAP code).

The results of the Phase II efforts are described in the balance of this report. The most important of the

Table 2. Conditions for Numerical Solutions in Current Phase II Portion of Study

			Liner:			
Case	Medium	Fracture Model	Thickness	Material	Remarks	
Н	Granite	Explicit shear cracks	Unlined			
J	NTS Tuff	Plasticity	Unlined			
K	NTS Tuff	Plasticity	1-ft	Concrete		
L	NTS Tuff	Explicit shear cracks	1-ft	Concrete		
М	NTS Tuff	Explicit shear cracks	2-in	Deformable steel	LAP code (linked FE/	
N	NTS Tuff	Explicit shear cracks	2-in + 2-ft	Deformable steel Concrete	FD) sol'ns	

1 kb planar step wave loading applied to upper boundary of grid



1' nominal zoning
used in all problems.

findings are the following:

- 1. Shear cracks (and presumably tensile cracks also) which form near the tunnel as a consequence of the dynamic loading can lead to non-uniformities in velocities near lined tunnels, and hence to stress concentrations in liners. These stress concentrations will need to be taken into consideration in the design of integral liners.
- 2. The LAP code provides a practical method for analyzing the coupled dynamic response of thin liners and the surrounding medium. The finite difference portion of the method is used to analyze free field motions and the medium response (including joint slippage and generation of explicit cracks), while the finite element portion is used to analyze the response of the liner. This combination avoids the necessity of using small cells (and small time steps) to resolve action in a relatively thin liner in a purely finite difference analysis.
- 3. Two-inch steel liners in 10-ft dia tunnels in tuff subjected to 1 kb stress wave loading will experience stresses which are large enough to cause inelastic deformation. Diametral strains of about 2-3 inches develop shortly after the tunnel liner is engulfed by a 1 kb step wave. Accelerations (relative to the center of mass of the tunnel) associated with these distortions are of the order of 1000-3000 g's.

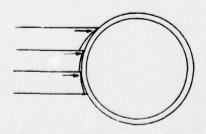
#### 2.2 RECOMMENDATIONS

Using the coupled LAP method, realistic liner systems, as well as new liner concepts, should now be analyzed to predict their response in various media and with various design parameters. LAP is able to treat fairly complex 2-D designs, and to generate dynamic response predictions which would be very

useful in making preliminary evaluations of new concepts, in examining dynamic failure mechanisms, and in helping to optimize design variables. The following specific work is recommended:

- 1. New design concepts The experimental evaluation of new design concepts is both expensive and time consuming.

  Small-scale experiments are useful for preliminary evaluations, but there are uncertainties and limitations in these tests relative to boundary conditions, material property simulation, and in observing potentially important dynamic phenomena on such small scale. LAP code solutions offer an alternative or supplementary approach for preliminary evaluations. Such solutions are particularly valuable in that they indicate the failure modes or weaknesses of new designs, thereby suggesting avenues for improvements.
- 2. Dynamic failure mechanisms The Phase I results indicate that relative displacements across joints will not usually be larger than a few inches under conditions of interest. (We refer here to the local motions which are discussed in the Phase I summary in Section 1 above.) Such motions can be accommodated by backpacking, but they become a much more serious concern with integral liners, which must resist any motion which would lead to significant relative displacements near the tunnel. In resisting such motions, large local concentrations of forces applied to the liner may develop, as indicated in the sketch below:



In addition to force concentrations due to motions along preexisting joints or cracks, the work in Phase II with explicit crack propagation suggests that cracking which is induced by the stress wave loading near the tunnel may also produce non-uniformities in loading on the liner. The dynamics of such force concentrations and/or non-uniformities need to be considered in liner design.

We had hoped, during Phase II, to be able to analyze one or more cases such as shown by the sketch on the preceding page. However, we did not get that far after completion of the LAP code implementation. In addition, we felt that such analyses should be performed after we could treat both explicit shear cracking and tensile cracking simultaneously in the Lagrangian code. We recommend that this additional modeling capability be added now, and that the local interactions of displacement discontinuities with tunnel liners then be analyzed to determine the stress concentrations in liners.

3. Parameter optimization - The LAP method offers a fairly efficient way to conduct series of analyses which can be used to guide the optimization of design variables so as to obtain the maximum useable tunnel volume for a given excavated volume. Survivability criteria can be specified, for example, in terms of liner fracture, or maximum allowable distortion, velocity, or acceleration. Solutions of this type can be obtained at modest cost, and the results used to construct curves showing sensitivity of liner response to the design variable, medium properties, etc.

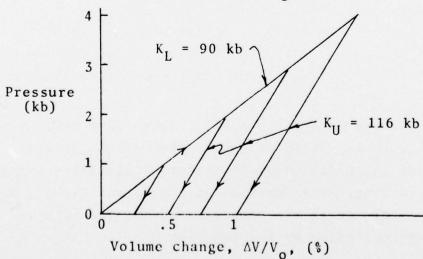
# 3. MATERIAL PROPERTIES FOR NUMERICAL SOLUTIONS

#### 3.1 TUFF

# 3.1.1 Equation of State

Emphasis in the Phase II portion of this study has been on tunnels in relatively soft geologic materials. NTS tuff was chosen as being representative of these softer materials. Fairly extensive constitutive property data are available for this material, as summarized in Ref. 3. These data show that the properties of NTS tuff vary considerably with depth, water content, etc. Because of this variability, and because the peak overpressures experienced by the tuff in our solutions would be only about 1 kb, a relatively simple, hydrostatic equation of state with constant, but different, loading and unloading moduli was adopted, based on the data in Ref. 3. We believe the important characteristics of deeply-buried tuff in the stress range of concern here are adequately represented by this approach.

A sketch of the behavior of the hydrostatic equation of state used in loading and unloading is shown below:



As indicated, the tuff loads with a bulk modulus,  $\rm K_L$  = 90 kb. It unloads (and reloads) with a bulk modulus,  $\rm K_U$  = 116 kb. This behavior was chosen to model hysteretic compaction of the material. Unloading from 4 kb, for example, results in a volume reduction of 1%, which is consistent with experimental hydrostatic loading curves and residual volume compaction data for several NTS tuffs.

A constant shear modulus during loading and unloading was used, based on experimental bulk modulus and longitudinal sound speed data from Ref. 3. The values used were 28 kb for the shear modulus and  $C_{\rm D}$  = 8500 fps.

# 3.1.2 Failure

The failure properties of the tuff were modeled in two ways: The first, which we refer to as the plasticity model, is the conventional method in which failure is assumed to manifest itself as a yielding phenomenon occurring on a plastic yield surface. The rationale for this model is that the material fails by developing numerous small cracks which simulate plastic behavior. The second failure model, which we refer to as the explicit shear crack model, represents a refinement of the plasticity approach. This method allows the formation of explicit shear cracks, along with appropriate stress adjustments.

Material failure data for NTS tuff, taken from Ref. 4, are shown in Figure 4. These data give the maximum shear stress,  $\tau$ , which any plane embedded in the material can experience without failing, as a function of the normal stress,  $\sigma_n$ , on that plane. For use in the numerical model, the data in Figure 4 were approximated by the function

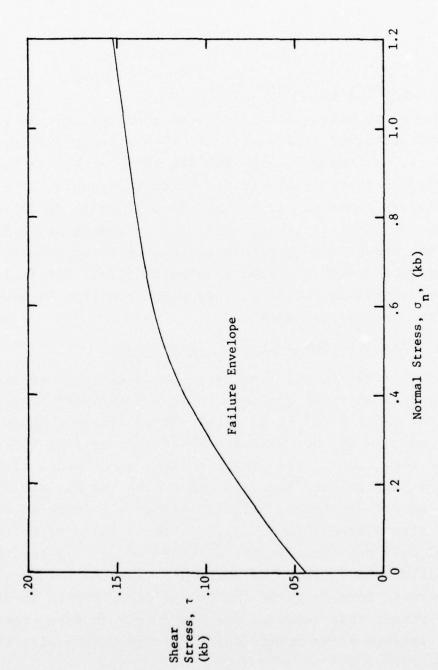


Figure 4. Maximum Shear Stress Which Can Be Withstood Across a Plane vs Normal Stress on Plane, NST Tuff (from Ref. 4)

$$\tau = \tau_{\infty} - ce^{\sigma} n^{/\sigma} o$$

$$\tau_{\infty} = .16 \text{ kb}$$

$$c = .115 \text{ kb}$$
(1)

# a. Plasticity Failure Model

 $\sigma_0 = .465 \text{ kb}$ 

where

The yield stress for the conventional plasticity failure model was obtained from eq. (1) by interpreting the normal stress,  $\sigma_n$ , as the pressure, and the shear stress as being proportional to the yield stress at that pressure. The proportionality constant was chosen to be 2, which (under conditions of uniaxial strain) results in yielding being initiated at the stress level where shear cracks first appear. Since the numerical solutions have a uniaxial strain far field boundary condition, a direct comparison can thus be made between the two failure models.

# b. Explicit Shear Crack Failure Model

In this model, material fails by developing explicit shear cracks whenever the shear stress across any plane exceeds the value given by eq. (1). After failure, appropriate stress adjustments are made in the cell to reflect the existence of the cracks. The explicit shear crack model also requires a post-failure function expressing the maximum shear stress across an already existing crack as a function of the normal stress across the crack. In the absence of better data, we used half the shear stress provided by eq. (1) for this post-failure condition. Note that in isotropic materials, shear cracks form in pairs: when the shear stress across one plane exceeds that required for a fracture to form, there is always another plane across which this criterion will also be

satisfied. Thus, in the code solutions, no cell ever develops a single shear crack; they always come in pairs. In field plots obtained from the numerical solutions, the orientation of the shear cracks is indicated by line segments which are drawn in each failed cell. If more than two shear cracks are formed in any cell, the plasticity failure model is thereafter adopted for the material in that cell.

Explicit tensile cracking has also been programmed in the WAVE-L Lagrangian code in connection with another application, but the combination of explicit tensile and shear cracking is not currently allowed in the code.

#### 3.2 GRANITE

For the one granite solution in Phase II (Case H), a linear elastic material model with bulk modulus, K = 512 kb, shear modulus, G = 293 kb, and density,  $\rho = 2.7 \text{ g/cm}^3$  was assumed. The shear failure surfaces for wet and dry granite joints, as determined in the Phase I effort, are reproduced in Figure 5. For Case H, we assumed that the shear failure surface for intact granite is the same as for a dry granite joint.

#### 3.3 CONCRETE

A simple, linear elastic equation of state was used to represent the concrete liners, with a bulk modulus,  $K=270~\mathrm{kb}$ , and a shear modulus,  $G=138~\mathrm{kb}$ . The concrete was not allowed to fail in these solutions.

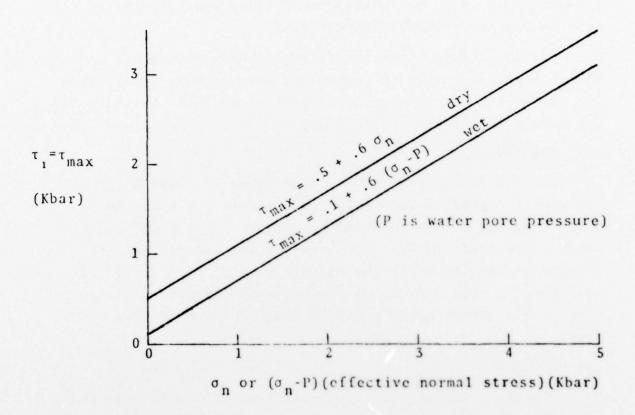


Figure 5. Shear Failure Surfaces for Wet and Dry Joints in Granite

#### 4. UNLINED AND CONCRETE-LINED TUNNELS

# 4.1 UNLINED TUNNEL IN GRANITE

Case H involved an unlined tunnel in granite. The granite was modeled as being linear elastic, failing only when shear cracks develop. Tensile failure was not allowed. This was a preliminary solution, intended primarily to exercise the explicit shear crack model for the first time. The results have some interest as a comparison for later cases. In addition, the problem parameters are similar to those in the small-scale experiments being conducted at Stanford Research Institute 5. Hence it offers some degree of code verification.

The two most prominent phenomena which are observed in the SRI experiments are (1) "flaking" at the springlines, and (2) long vertical cracks emanating from the springline region, as sketched in Figure 6.

Case H was run to 5.24 msec, which is about 2 msec after the stress wave strikes the top of the tunnel. Figures 7, 8, and 9 show the final grid configuration, velocity field, and principal stress field. Failed cells are denoted in the grid by line segments (aligned with the directions of the shear cracks) at the cell centers. Extensive shear fracture has occurred at the springlines in Figure 7, and flaking of the tunnel wall would result if the solution were continued. This tendency is seen in the effects of the stress relief afforded by the shear cracking in the velocity field (Figure 8). At 5.24 msec, however, the shear cracking is not propagating out of the springline region to form the long vertical cracks seen in the SRI experiments (as sketched in Figure 6). Rather, the stress plot in Figure 9 shows that significant tensile stresses

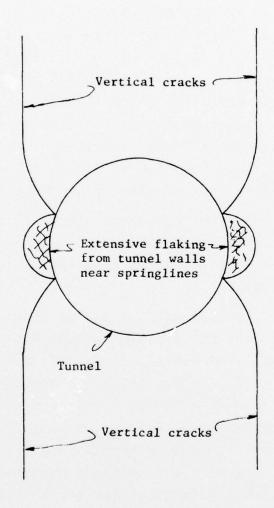


Figure 6. Sketch of Predominant Fracture Patterns Seen in SRI Small-Scale Tests

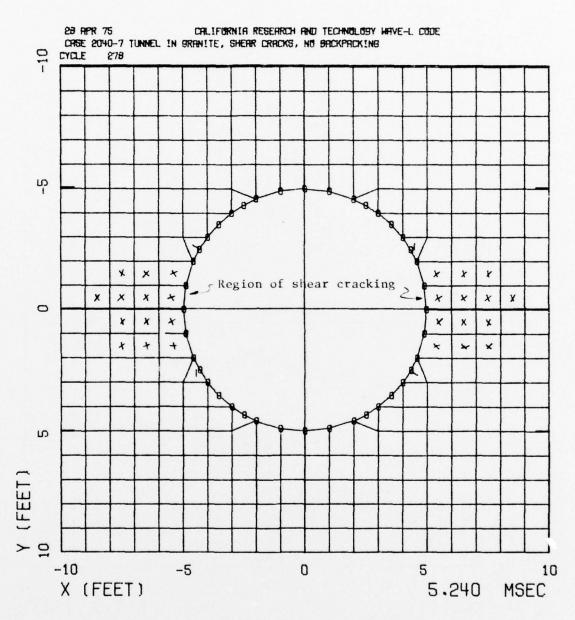


Figure 7. Case H - Unlined Tunnel in Granite with Explicit Shear Crack Failure Model.
Final Grid Configuration (at 5.2 msec)

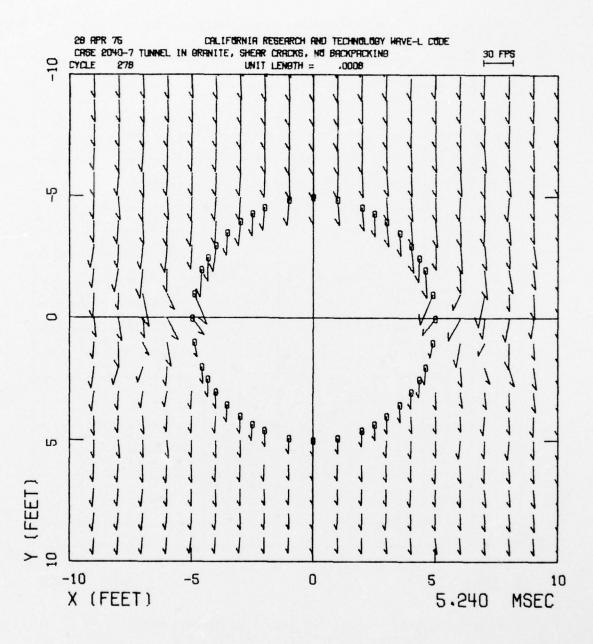
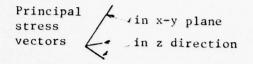


Figure 8. Case H - Unlined Tunnel in Granite with Explicit Shear Crack Model. Final Velocity Field (at 5.2 msec)



Vectors having rightward components are compressive; leftward vectors are tensile

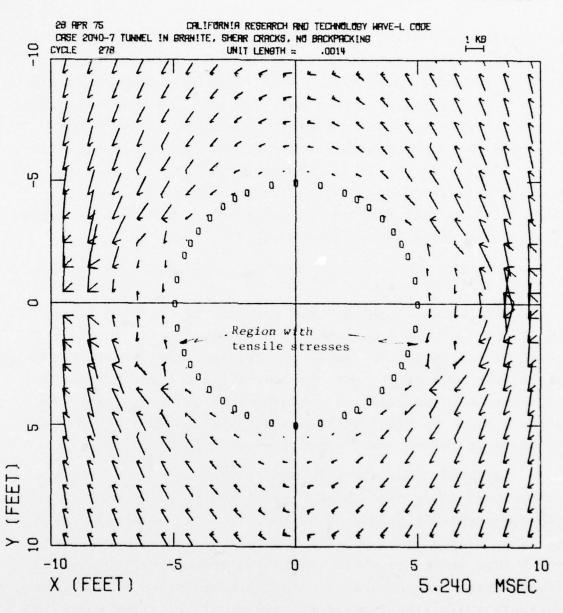


Figure 9. Case H - Unlined Tunnel in Granite with Explicit Shear Crack Model. Final Principal Stress Field (at 5.2 msec)

are developing in the regions where vertical cracks should initiate. These tensile stresses are of sufficient magnitude to produce cracking if a tensile failure model were present in this solution. This suggests that the vertical cracks which are observed experimentally are caused not by shear failure, as had been previously assumed, but by tensile failure. The stress relief allowed when the shear crack forms in the springline region produces tension in the surrounding material, and this tension can cause fractures which propagate to form the observed vertical cracks.

# 4.2 CONCRETE LINERS IN TUFF - COMPARISONS SHOWING EFFECTS OF DIFFERENT FAILURE MODELS

Cases K and L examined the response of concrete liners in NTS tuff. Case K contained a 1-ft linear elastic concrete liner in tuff with the plasticity failure model. Case L contained the same liner, but the explicit shear crack failure model was used for the tuff. Comparison of the results from Cases K and L provides some indication of whether or not use of the more refined explicit crack model is necessary.

Figure 10 shows the grid used for these cases. The concrete liner is denoted by the shaded region. Figure 11 shows the computational grid in Case L at 10 msec, after the tunnel has been completely enveloped by the 1 kb stress wave. Cells which have developed shear cracks are denoted by the crossed line segments in the cells, with the orientation of the line segments indicating the directionality of the shear cracks. It is seen that most of the tuff cells in the problem have failed.

Figures 12 and 13 compare the stress fields for Cases K and L at 10 msec. Both of the failure models have resulted in

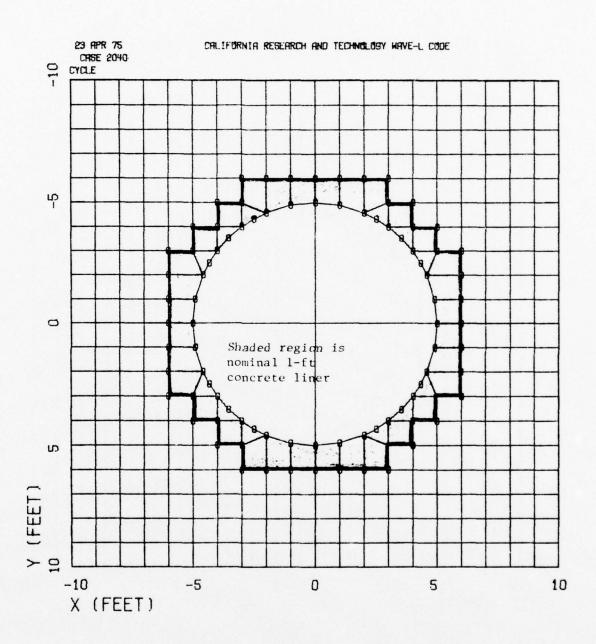


Figure 10. Computational Grid for Concrete Liners in Tuff (Cases K and L)

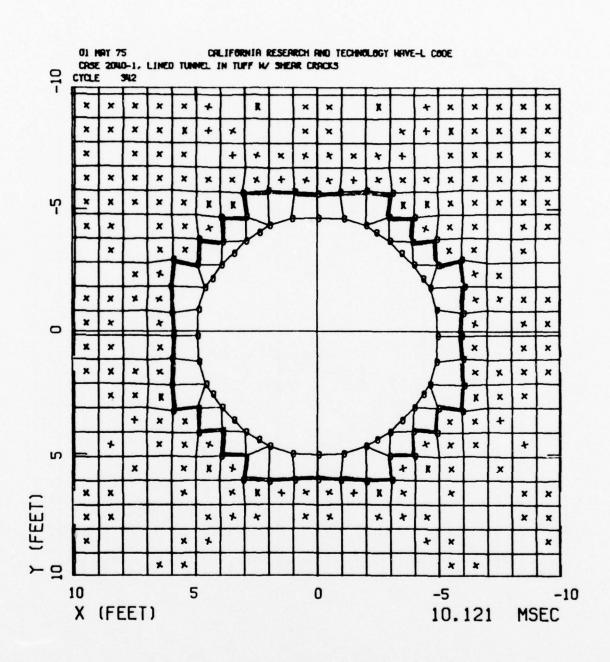


Figure 11. Case L - Concrete-Lined Tunnel in Tuff with Explicit Shear Crack Failure Model. Grid at 10.1 msec, Showing Pattern of Shear Cracks

Rightward components are compressive

Principal stress vectors in z direction

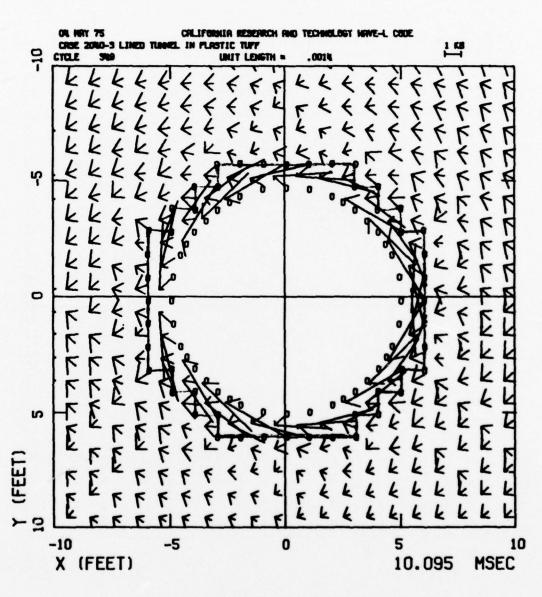


Figure 12. Case K - Concrete-Lined Tunnel in Tuff with Plasticity Failure Model.
Principal Stress Field at 10.1 msec.

Rightward components are compressive



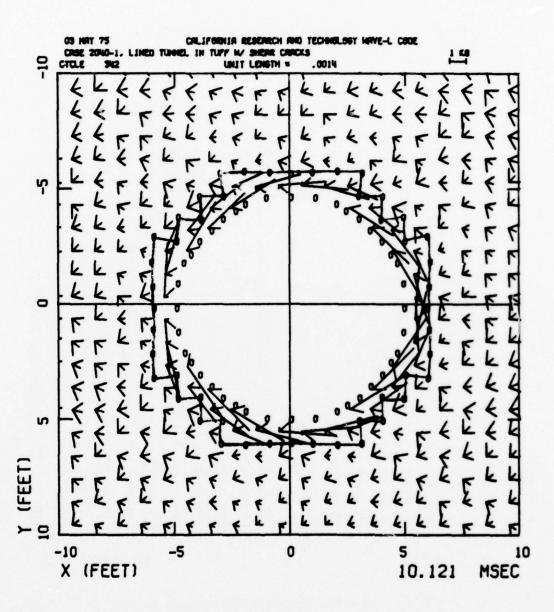


Figure 13. Case L - Concrete-Lined Tunnel in Tuff with Explicit Shear Crack Failure Model. Principal Stress Field at 10.1 msec.

essentially the same stress fields. The concrete liner in both cases has been compressed, producing a tangential (hoop) stress of about 3 kb. The principal stresses in the tuff are about 1 kb. Note that the principal stress components in the tuff adjacent to the liners are approximately equal, indicating that the liners are being subjected to a uniform pressure around their perimeters.

Figures 14 and 15 show the velocity fields for the two lined cases at 10 msec, and here we see that the two methods of treating failure have produced significant differences in the results. In Case K (Figure 14), the tunnel and backpacking have acquired a fairly uniform velocity, about the same as that of the surrounding tuff. In Case L (Figure 15), the explicit shear crack model has resulted in distinctly non-uniform velocities. In particular, note the large inward velocities on the tunnel-liner interface at about the 10:30 and 1:30 positions.

These comparative results indicate that the plasticity and explicit shear crack models for material failure may produce substantially different local velocities and hence displacements near the liner. In particular, the introduction of explicit shear cracks appears to lead to non-uniformities in the velocity field near the liner. This may cause stress concentrations which will need to be considered in the design of liners. To properly determine these concentrations, material models and numerical methods which allow the generation of discontinuities (i.e., both shear and tensile cracks) will be needed.

### 4.3 UNLINED VS CONCRETE-LINED TUNNELS IN TUFF

Case J consisted of an unlined tunnel in tuff. The re-

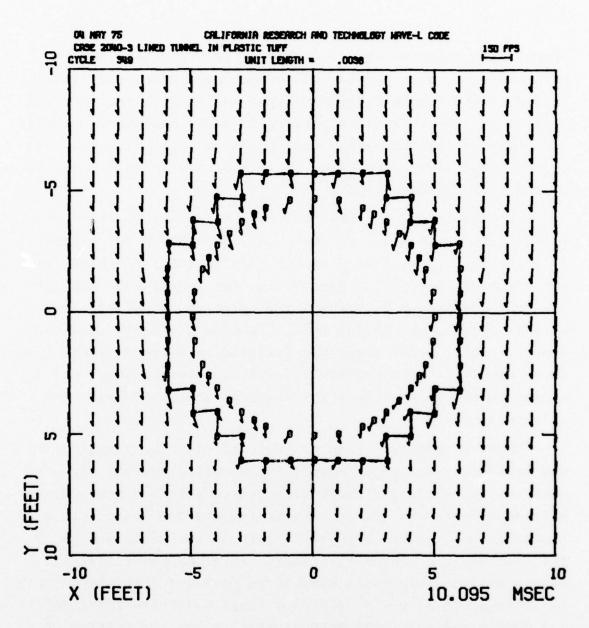


Figure 14. Case K - Concrete-Lined Tunnel in Tuff with Plasticity Failure Model.
Velocity Field at 10.1 msec.

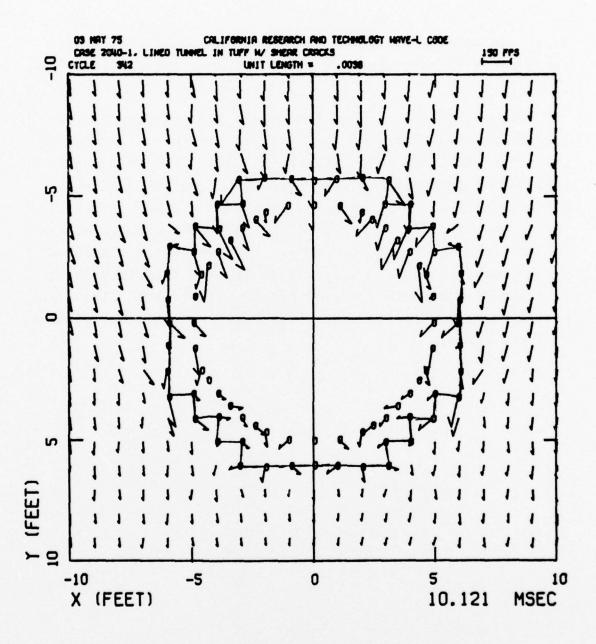


Figure 15. Case L - Concrete-Lined Tunnel in Tuff with Explicit Shear Crack Failure Model. Velocity Field at 10.1 msec.

sults can be directly compared with the preceding concretelined cases in tuff (Cases K and L) to show the action of the concrete liner.

Figures 16 and 17 show the stress and velocity fields for the unlined Case J at the same time as the corresponding plots for the lined cases (Figures 12-15). The unlined tunnel, rather than being accelerated to the velocity of the surrounding tuff, has developed significant inward velocities (at about twice the velocity of the surrounding tuff) and is collapsing. The strong tangential stresses which developed in the concrete liner (e.g., Figure 12) are totally missing in the tuff around the unlined tunnel (Figure 16). This tangential compression, of course, is what prevents the collapse of lined tunnels.

Rightward components are compressive

Principal stress vectors in z direction

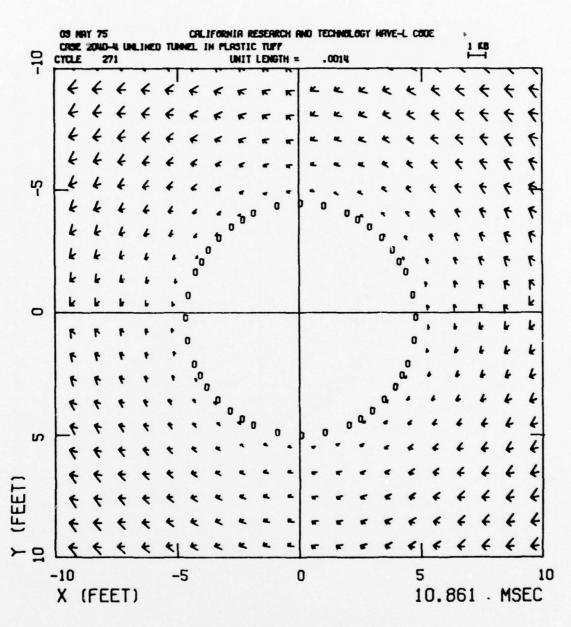


Figure 16. Case J - Unlined Tunnel in Tuff with Plasticity Model. Principal Stress Field at 10.9 msec.

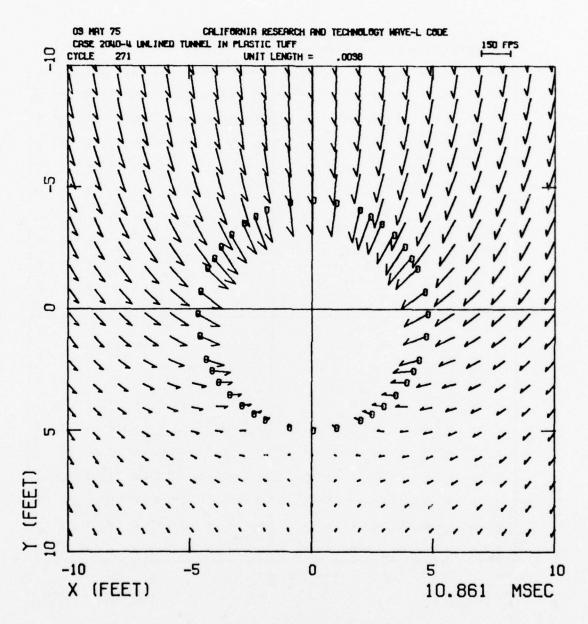


Figure 17. Case J - Unlined Tunnel in Tuff with Plasticity Failure Model.
Velocity Field at 10.9 msec.

# 5. COUPLED FINITE DIFFERENCE/FINITE ELEMENT LAP CODE FOR ANALYSIS OF THIN LINERS

Thick liners can be represented using a finite difference code, as is seen by the examples in Cases K and L in Section 4.2 above. It is not practical, however, to treat thin liners, such as steel, by the finite difference method because relatively small cells must be used to resolve action in the thin steel section. The combination of small cells and high sound speedin steel lead to time steps which are too small for fairly long-duration buried structure analyses.

For convenience, steel liners are sometimes represented as rigid bodies in buried structure analyses. This was the approach taken in Phase I of this study. It is a reasonable approach so long as elastic distortion of the liner does not cause substantial stress adjustments, or allow small joint motions in the nearby medium. Unfortunately, test results indicate that elastic diametral strains are indeed sufficient to be of concern in analyses of integral liners. Thus blocks which are in contact with integral liners may be able to shift slightly, producing non-uniform stresses along the medium/liner interface, and perhaps substantial stress concentrations in the liner. These will need to be taken into consideration in the design of integral liners.

Our approach to this problem has been to implement a coupled finite difference/finite element numerical method, which we will call LAP, for Linked Analysis Program. In this coupled method, the earth medium is represented by the Lagrangian finite difference WAVE-L code, which allows joint slippage and stress accommodations to occur around the liner, and which treats the far field and near field ground motions in

efficient manner. The integral structural liner is represented by an adaptation of the finite element SAP IV code<sup>6</sup>, which can describe the displacements of the liner and the dynamics of the stress field in the liner. Concrete backing for a steel liner can be treated using either the finite element of the finite difference portion of the LAP method.

The finite difference and finite element portions of LAP are coupled on a cycle-by-cycle basis across a specified interface (usually the medium/liner interface). In each integration cycle, the finite difference code provides forces across the interface to the finite element code, which in turn provides displacements back across the interface. This linked LAP method is now operational, and it was used to generate the solutions with steel liners (Cases M and N) which are described in the following section.

#### 6. DEFORMABLE STEEL LINERS

For the initial LAP code analyses, two solutions were obtained for steel liners in tuff (Cases M and N). In both of these cases, two-inch thick steel liners were used in a 10-ft dia tunnel in tuff. The steel was considered to be linearly elastic (i.e., with no yield or failure criterion). The tuff was modeled using the explicit shear crack failure model described in Section 3.

The liner was represented in the finite element portion of the LAP code by 32 beam finite elements, coupled to the finite difference cells at the interface node points.

# 6.1 TWO-INCH STEEL LINER IN TUFF (CASE M)

In this problem, the steel liner was in direct contact with the tuff medium. The solution was run to 15 msec. Figures 18, 19, and 20 show the computational grid velocity field, and principal stress fields at 7.5 msec, as the stress wave is engulfing the tunnel. Figures 21, 22, and 23 show the same plots at 14.5 msec, with the tunnel completely engulfed by the step wave. The pattern of shear cracks is similar to that obtained in the earlier solution of a concrete liner in tuff (Case L, Figure 11).

Time histories of the steel liner response were obtained from the finite element portion of LAP at the stations identified in Figure 24. Figures 25 to 29 show the hoop stress histories on the inner surface (i.e., the free surface) and on the outer surface (the steel/tuff interface). These stresses exceed a nominal yield strength of steel (say 10 kb, or 150 ksi) after about 12 msec, so permanent deformation and probably failure of the liner will occur. At the end of the solution

at 15 msec, the hoop stress is beginning to level off as it approaches about 30 kb (450 ksi), which would be the stress level reached in a static solution of this problem.

Figures 30 to 35 show displacement and velocity histories at the top and bottom stations, and at the springline of the liner. The vertical displacements and velocities are relative to the center of mass of the steel liner. Note that the top station (25) has been pushed down towards the center of mass about 4 inches by 15 msec. The bottom station (9) first moves up, relative to the mass center, then also moves downward, to about 1 inch by 15 msec. The springline station (1) experiences about 1-in outward radial displacement by 15 msec (about 2-in diametral strain). These motions occur at velocities, relative to the center of mass, in the range up to about 150 fps. Slopes of the velocity histories indicate relative accelerations of the order of 1000-3000 g's.

# 6.2 TWO-INCH STEEL LINER BACKED BY TWO FEET OF CONCRETE IN TUFF (CASE N)

This problem was identical to the preceding Case M, except that the steel liner was backed by about two feet of concrete. The concrete was treated by the finite difference portion of the code, so the finite difference/finite element interface was between the steel liner and the concrete. Figure 36 shows the computational grid at 7.5 msec, as the stress wave was engulfing the tunnel. The concrete backing is shown by shading in this plot. Figure 37 and 38 show the velocity and principal stress fields at this same time.

The solution was carried out until 9.5 msec, and the final grid, velocity field, and principal stress field are shown in Figures 39, 40, and 41. The stress level in the concrete had reached about 3-4 kb by this time, and was beginning to rise

sharply in the steel. We did not continue the solution further.

An alternative to placing the finite difference/finite element interface between the steel and concrete would be to include the concrete in the finite element portion of the solution. This would be somewhat more efficient, but it would sacrifice the generality in treatment of material properties, fracture, and explicit crack propagation which is available in the finite difference code.

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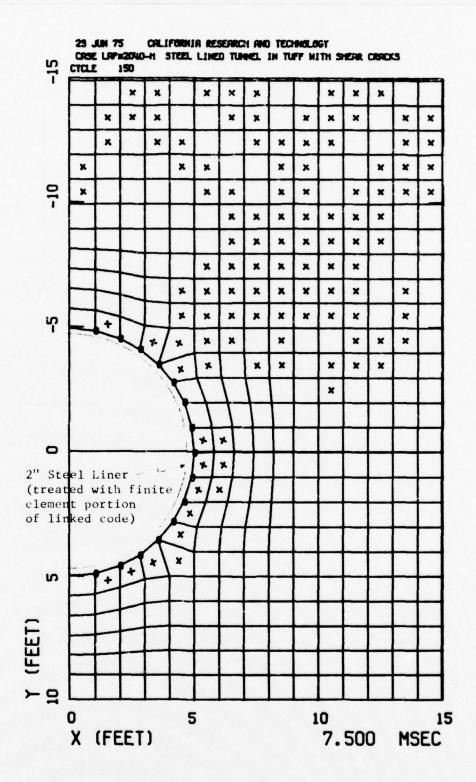


Figure 18. Computational Grid for Lagrangian Finite
Difference Portion of LAP Code Solution
for Case M - 2" Steel Liner in Tuff with
Explicit Shear Crack Failure Model.
(t = 7.5 msec)

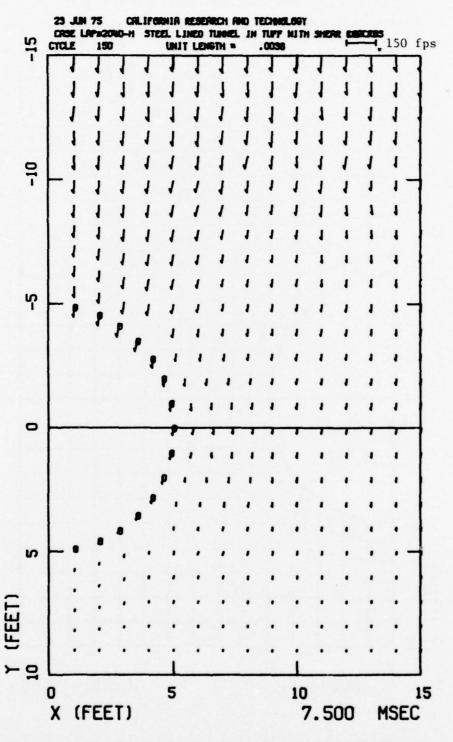


Figure 19. Velocity Field for Lagrangian Finite Difference Portion of LAP Code Solution for Case M - 2" Steel Liner in Tuff with Explicit Shear Crack Failure Model (t = 7.5 msec)

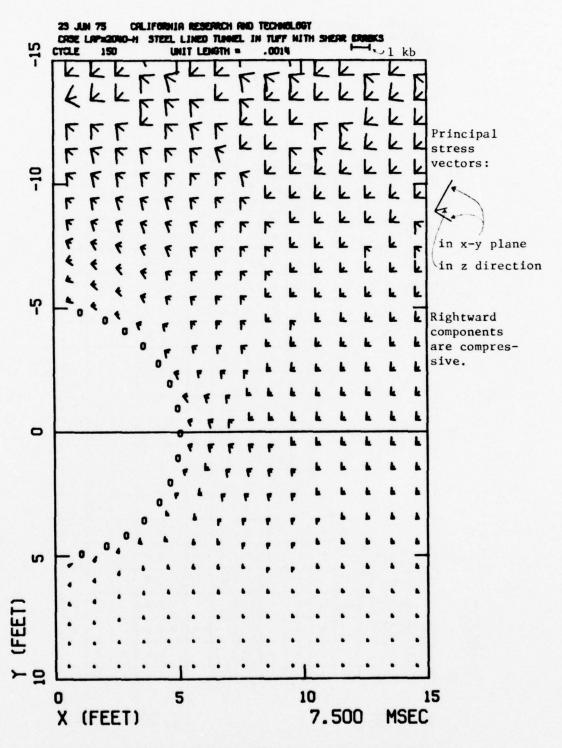


Figure 20. Principal Stress Field for Lagrangian Finite
Difference Portion of LAP Code Solution for
Case M - 2" Steel Liner in Tuff with Explicit
Shear Crack Failure Model. (t = 7.5 mesec)

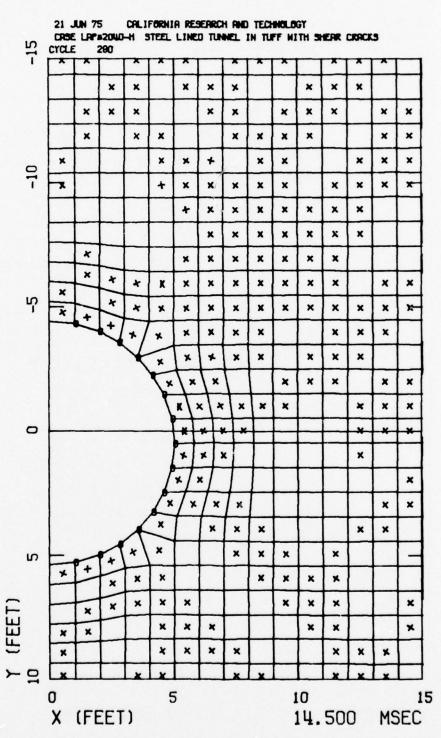


Figure 21. Computational Grid for Lagrangian Finite
Difference Portion of LAP Code Solution for
Case M - 2" Steel Liner in Tuff with Explicit
Shear Crack Failure Model (t = 14.5 msec)

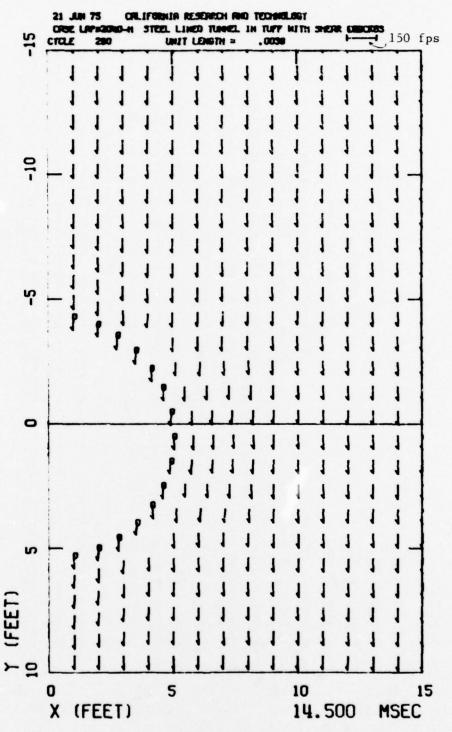


Figure 22. Velocity Field for Lagrangian Finite Difference Portion of LAP Code Solution for Case M - 2" Steel Liner in Tuff with Explicit Shear Crack Failure Model (t = 14.5 msec)

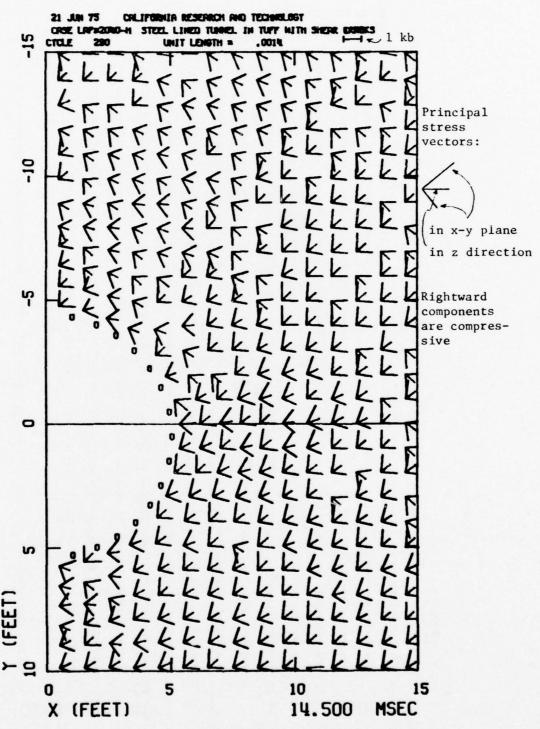


Figure 23. Principal Stress Field for Lagrangian Finite
Difference Portion of LAP Code Solution for
Case M - 2" Steel Liner in Tuff with Explicit
Shear Crack Failure Model. (t = 14.5 msec)

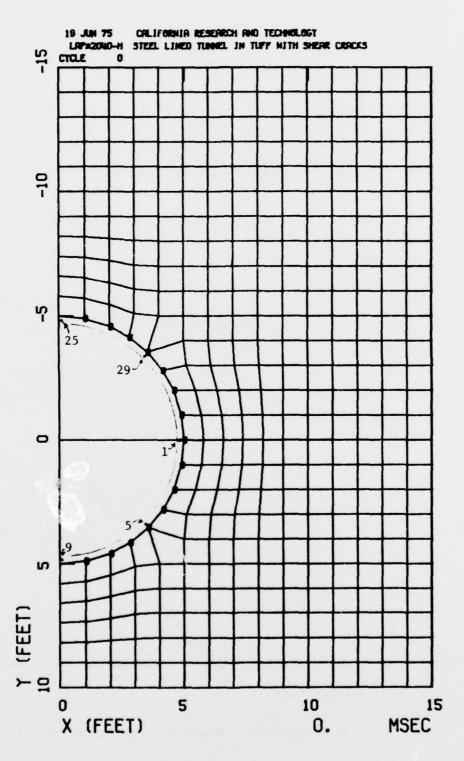


Figure 24. Locations of Time-History Stations for Plots in Figures 25-29 (Case M - 2" Steel Liner in Tuff)

# CALIFORNIA RESERRCH AND TECHNOLOGY, INC. LAP-2000-H STEEL LINER RESPONSE 23 JN 75 400.0 300.0 Station 25 Outer surface hoop stress HOOP STRESS,KSI 100.0 200.0 Inner surface hoop stress ö 5 10 15 TIME MSEC

Figure 25. Compressive Hoop Stress History at Station 25 in 2" Steel Liner. Case M - Steel Liner in Tuff

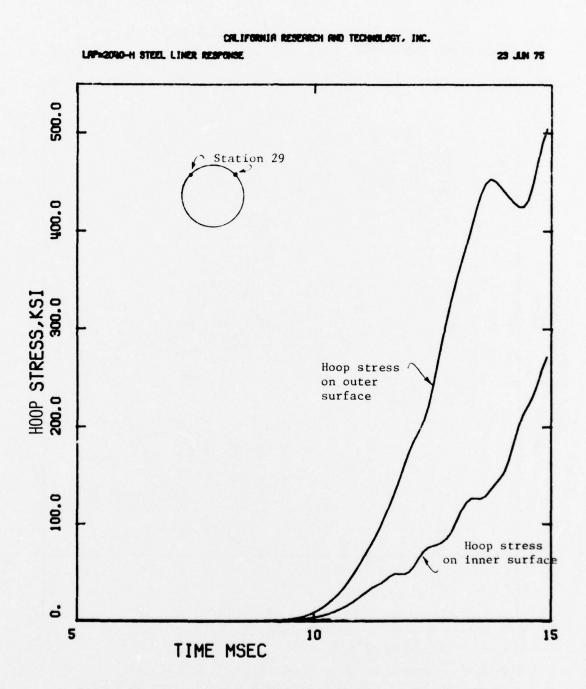


Figure 26. Compressive Hoop Stress History at Station 29 in 2" Steel Liner. Case M - Steel Liner in Tuff

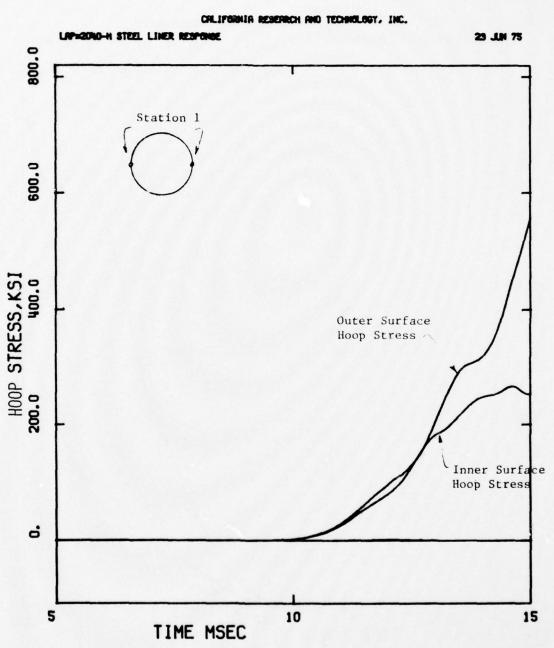


Figure 27. Compressive Hoop Stress History at Station 1 in 2" Steel Liner. Case M - Steel Liner in Tuff

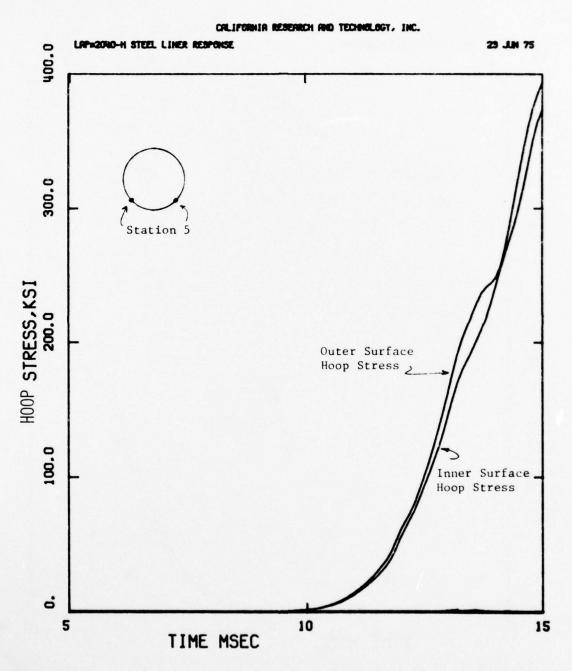


Figure 28. Compressive Hoop Stress History at Station 5 in 2" Steel Liner. Case M - Steel Liner in Tuff

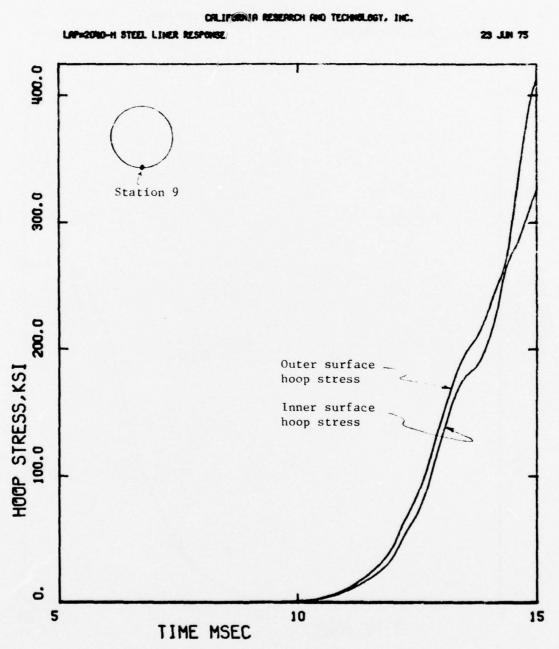


Figure 29. Compressive Hoop Stress History at Station 9 in 2" Steel Liner. Case M - Steel Liner in Tuff

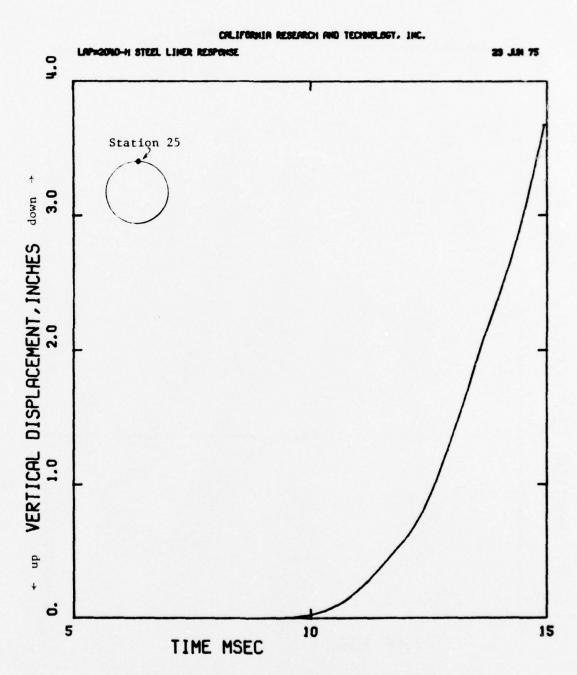


Figure 30. Vertical Displacement (Relative to Center of Mass of Steel Liner) of Station 25.

Case M - 2" Steel Liner in Tuff

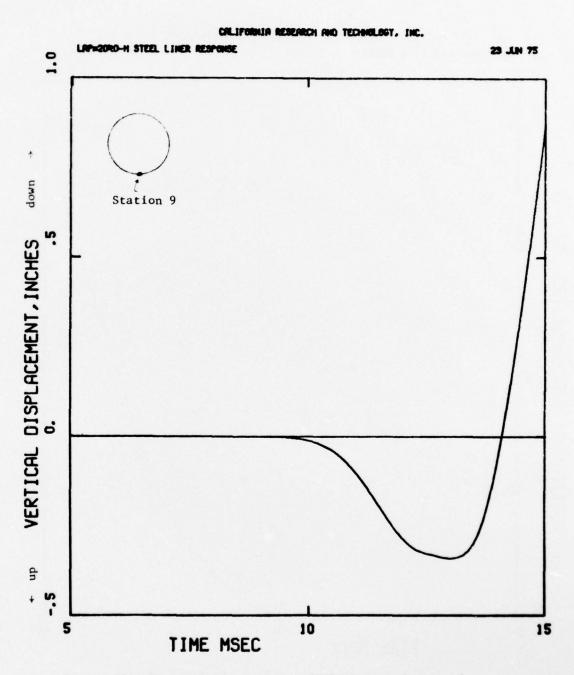


Figure 31. Vertical Displacement (Relative to Center of Mass of Steel Liner) of Station 9.
Case M - 2" Steel Liner in Tuff

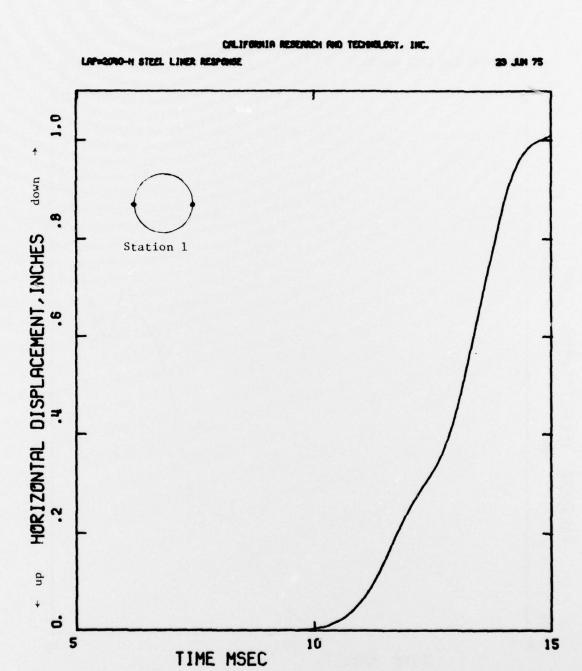


Figure 32. Horizontal (Radial) Displacement of Station 1 in 2" Steel Liner. Case M - Steel Liner in Tuff

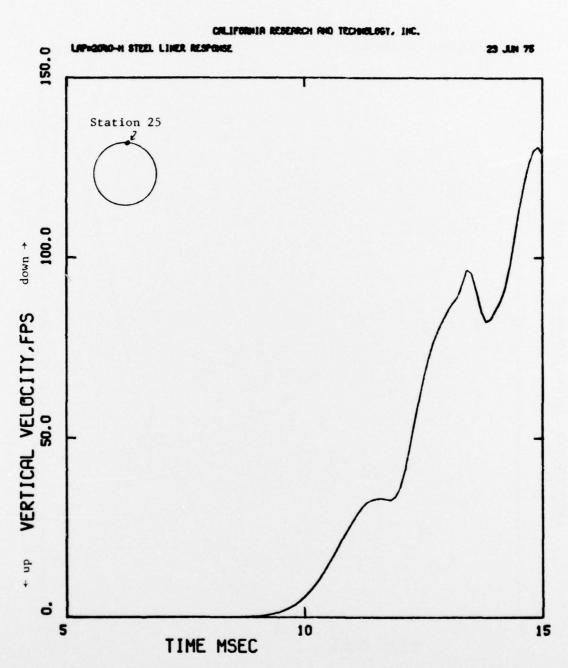


Figure 33. Vertical Velocity of Station 25 (Relative to Center of Mass of Steel Liner). Case M - 2" Steel Liner in Tuff

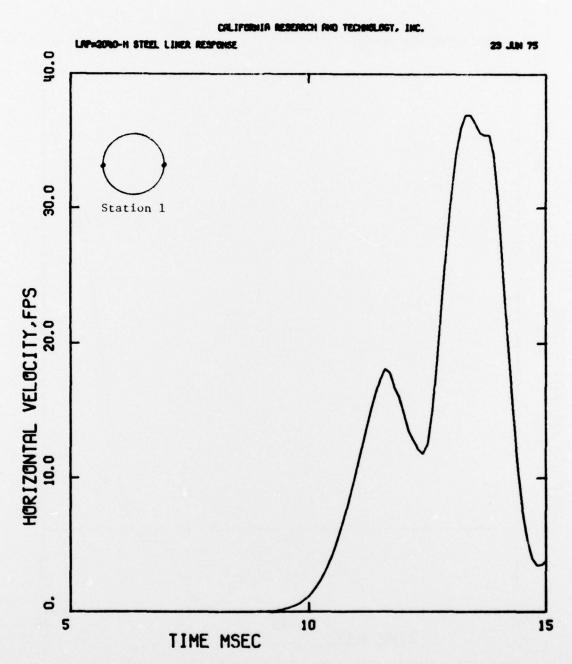


Figure 34. Horizontal (Radial) Velocity of Station 1 in 2" Steel Liner. Case M - Steel Liner in Tuff

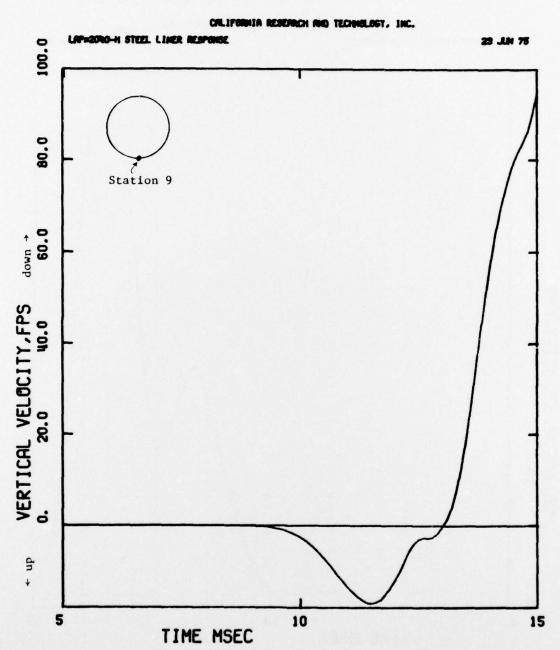


Figure 35. Vertical Velocity of Station 9 (Relative to Center of Mass of Steel Liner). Case M - 2" Steel Liner in Tuff

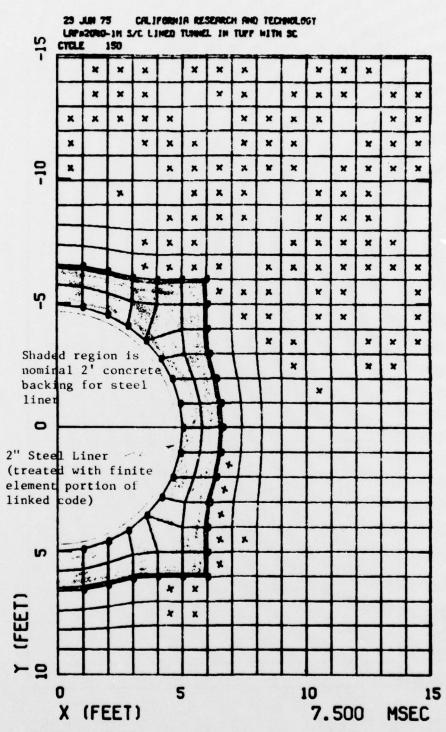


Figure 36. Computational Grid for Lagrangian Finite
Difference Portion of LAP Code Solution
for Case N - 2" Steel Liner with 2' Concrete
Backing in Tuff with Explicit Shear Crack
Failure Model (t = 7.5 msec)

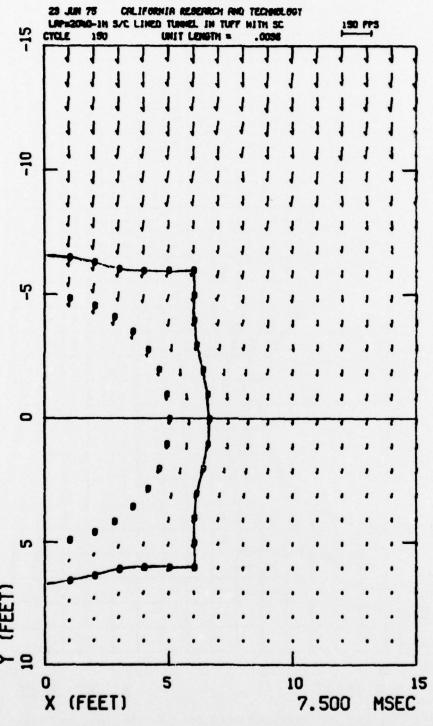


Figure 37. Velocity Field for Lagrangian Finite Difference
Portion of LAP Code Solution for Case N 2" Steel Liner with 2' Concrete Backing in Tuff
with Explicit Shear Crack Failure Model
(t = 7.5 msec)

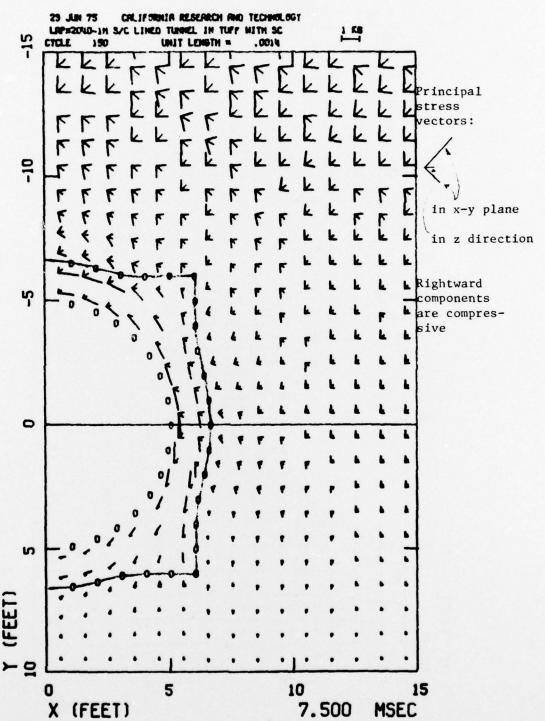


Figure 38. Principal Stress Field for Lagrangian Finite
Difference Portion of LAP Code Solution for
Case M - 2" Steel Liner in Tuff with Explicit
Shear Crack Failure Model. (t = 7.5 msec)

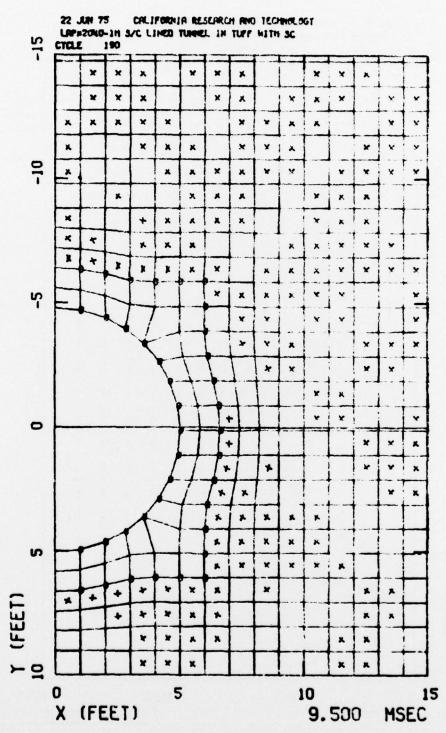


Figure 39. Computational Grid for Lagrangian Finite
Difference Portion of LAP Code Solution
for Case N - 2" Steel Liner with 2' Concrete
Backing in Tuff with Explicit Shear Crack
Failure Model (t = 9.5 msec)

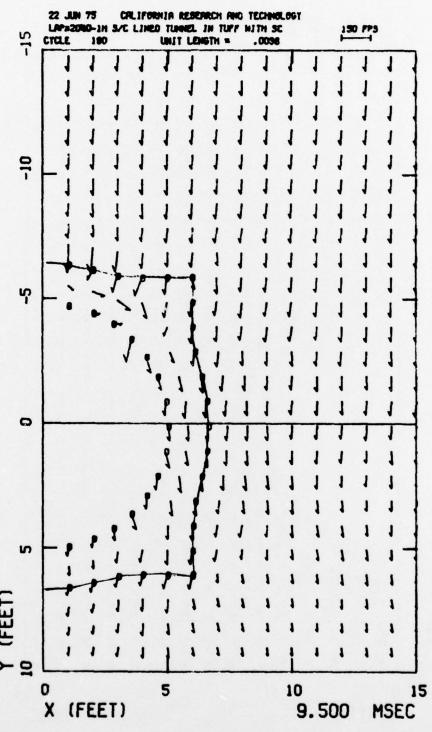


Figure 40. Velocity Field for Lagrangian Finite Difference
Portion of LAP Code Solution for Case N - 2" Steel
Liner with 2' Concrete Backing in Tuff with Explicit
Shear Crack Failure Model. (t = 9.5 msec)

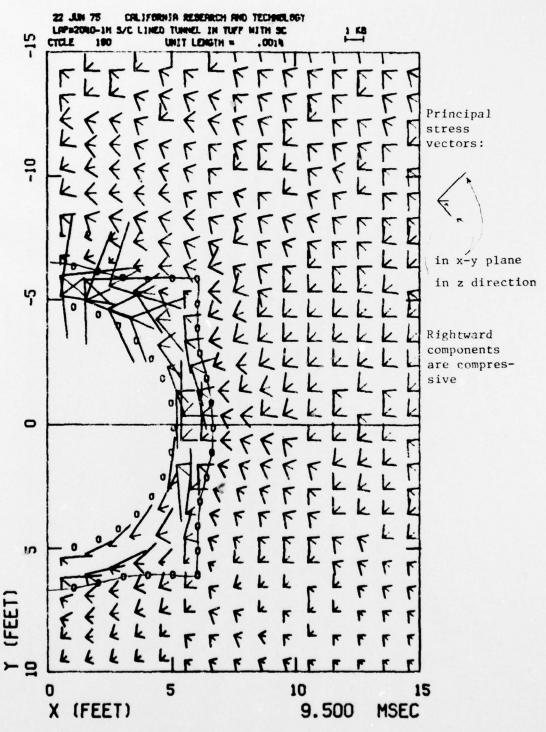


Figure 41. Principal Stress Field for Lagrangian Finite
Difference Portion of LAP Code Solution for
Case M - 2" Steel Liner in Tuff with Explicit
Shear Crack Failure Model (t = 9.5 msec)

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ATTN: George R. Abrahamson ATTN: Burt R. Gasten

Systems, Science and Software, Inc.
ATTN: Ted Cherry
ATTN: Technical Library
ATTN: Thomas D. Riney
ATTN: Donald R. Grine

Terra Tek, Inc. ATTN: Technical Library ATTN: Sidney Green

Tetra Tech., Inc.
ATTN: Li-San Hwang
ATTN: Technical Library

TRW Defense & Space Sys. Group
ATTN: Pravin Bhutta, R1-1104
2 cy ATTN: Peter K. Dai, R1/2170
ATTN: Tech. Info. Center/S-1930

## DEPARTMENT OF DEFENSE CONTRACTORS (Continued)

TRW Defense & Space Sys. Group San Bernardino Operations ATTN: E. Y. Wong, 527/712

Universal Analytics, Inc. ATTN: E. I. Field

The Eric H. Wang Civil Engineering Rsch. Fac. University Station

The University of New Mexico ATTN: Neal Baum ATTN: Larry Bickle

Weidlinger Assoc. Consulting Engineers ATTN: Melvin L. Baron

Weidlinger Assoc. Consulting Engineers ATTN: J. Isenberg

Westinghouse Electric Corp.

Marine Division
ATTN: W. A. Volz